

Application of new Monte Carlo method for inversion of prestack seismic data

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Overview

- Motivation
- Introduction
 - Bayes theorem
 - Stochastic inference methods
- Methodology
 - Greedy annealed importance sampling (GAIS)
- Application of GAIS on seismic inversion
 - Example 1: HRS demo data
 - Example 2: China data set
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Motivation

- Goal: estimate a log of rock properties as a function of two-way vertical travel time or depth
- Problem: limited wells
- Purpose of seismic inversion: derive a pseudo-log to fill in the gaps between wells

Geophysical inversion has non unique solutions



Derive models with uncertainties

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Introduction

Posterior pdf

Likelihood

Prior pdf

Bayes theorem:

$$P(\mathbf{x}|\mathbf{d}) = \frac{P(\mathbf{d}|\mathbf{x})P(\mathbf{x})}{P(\mathbf{d})}$$

$$E(\mathbf{x}) = (\mathbf{d} - \mathbf{g}(\mathbf{x}))^T \mathbf{C}_D^{-1} (\mathbf{d} - \mathbf{g}(\mathbf{x}))$$

$$P(\mathbf{d}|\mathbf{x}) \propto \exp(-E(\mathbf{x}))$$

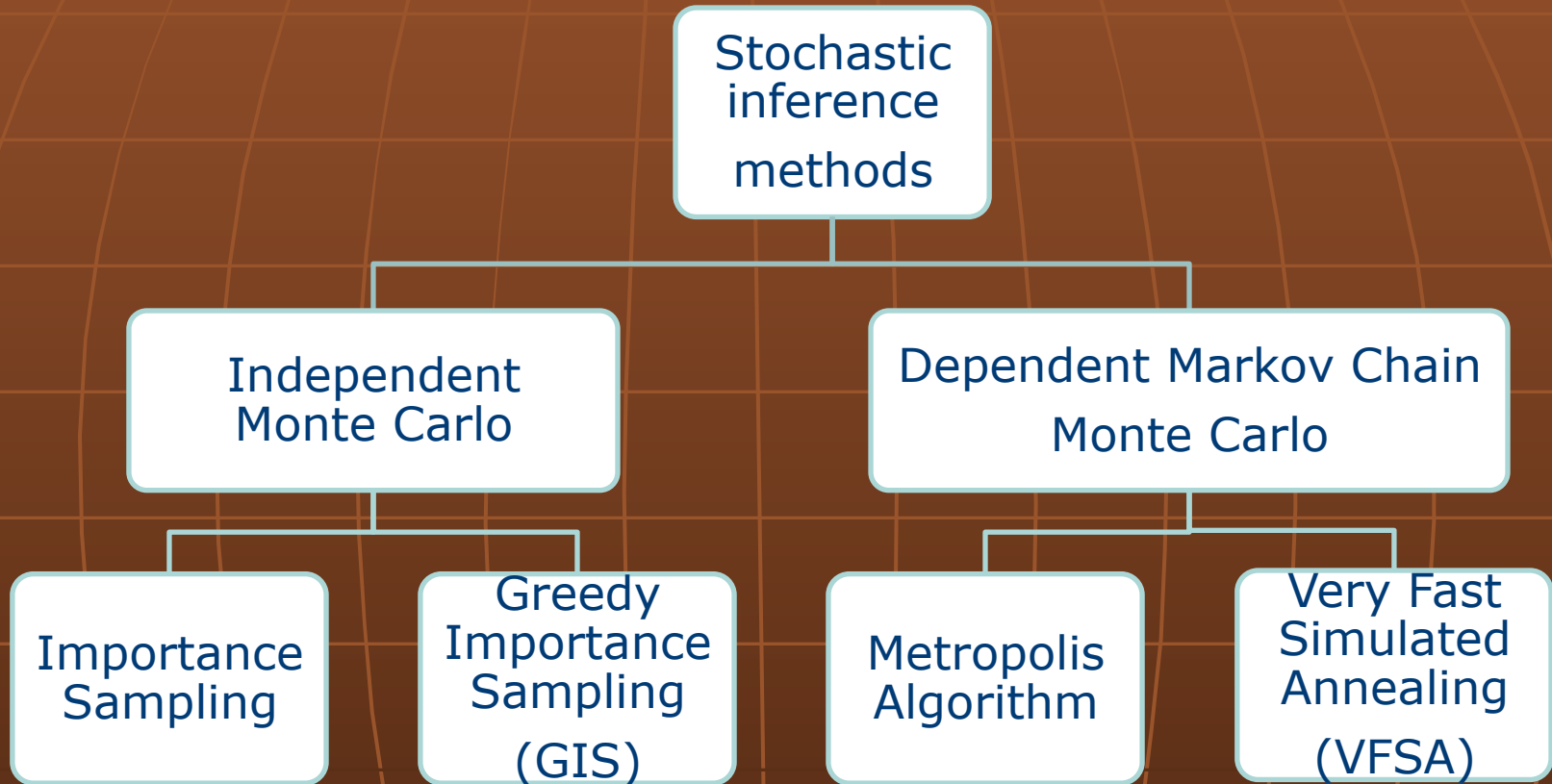
Draw samples from Prior distribution

Stochastic inference methods

Samples in Posterior distribution

$$\langle \mathbf{x} \rangle = \sum \mathbf{x} P(\mathbf{x} | \mathbf{d})$$

Introduction



(Southey and Shuurmans 2002)

Introduction

Metropolis-Hastings

Start at \mathbf{x}_0 with Error $E(\mathbf{x}_0)$

$\mathbf{x}_1 = \mathbf{x}_0 + D\mathbf{x}; E(\mathbf{x}_1)$

Accept \mathbf{x}_1 with Prob = $\exp(-DE/T)$

Weigh each model with probability and then evaluate the integrals to estimate the marginal PPD, posterior mean, covariance and correlation matrices

Introduction

Very Fast Simulated Annealing

Start at \mathbf{x}_0 with Error $E(\mathbf{x}_0)$

$$\mathbf{x}_1 = \mathbf{x}_0 + D\mathbf{x}; E(\mathbf{x}_1)$$

Reduce temperature

temperature dependent

Accept \mathbf{x}_1 with Prob = $\exp(-DE/T)$

Weigh each model with probability and then evaluate the integrals to estimate the marginal PPD, posterior mean, covariance and correlation matrices

Introduction

Importance Sampling

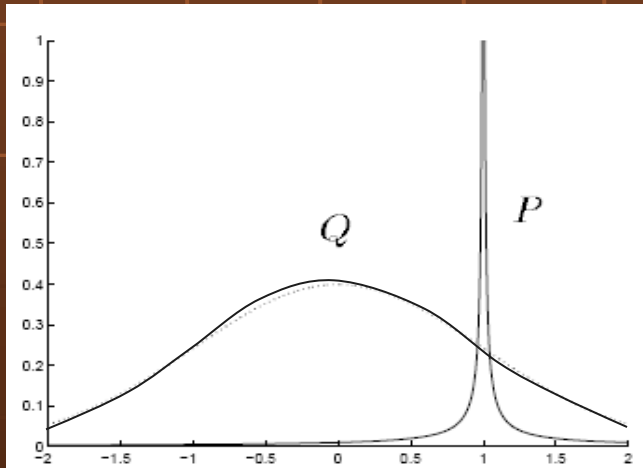
- Draw samples from prior distribution Q , assign weights

$w_i = P/Q$, estimate expectation:

$$E_{P(x)}f(x) = \sum_{i=1}^{i=n} f(x_i)w(x_i)/n$$

- Problem:

Q misses high probability regions of P



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Stochastic inference methods

Methods	Algorithm	Acceptance Rule	Pros and cons
Metropolis Algorithm	Updating sample using Markov Chain	Change of misfit ΔE	Accurate estimation, Computationally slow
Very Fast Simulated Annealing	Updating sample using Markov Chain, prior distribution temperature dependent	Change of misfit ΔE	Fast, biased estimation of uncertainties due to continuous change of proposal distribution with iterations
Importance Sampling	Randomly drawing samples from prior distribution	All accepted, but weighted $w = \frac{P(\mathbf{x})}{Q(\mathbf{x})}$	Fails, if prior distribution Q miss high probability region of posterior distribution P

Methodology

Greedy Importance Sampling - GIS

VFSA(T1) VFSA(Ti) VFSA(Tn)

$$(x_1, \dots, x_i, \dots, x_n) \quad Q$$

$$B_i = (x_{i,1}, \dots, x_{i,j}, \dots, x_{i,m})$$

local maximum of $|f(x)P(x)|$
or m-1 steps

$$w_i(x_j) = \frac{P(x_j)}{Q(x_i)} \alpha_{ij}$$

$$\sum_{x_i \in X} \alpha_{ij} I_{ij} = 1$$

$$E_{P(x)} f(x) = \frac{1}{n} \sum_{i=1}^n \sum_{k=1}^m f(x_{i,k}) w_i(x_k)$$

(Southey and Shuurmans 2002)

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- Methodology:
 - Greedy search for important region of \mathbf{X}
 - Each independent block contains one or two important points from \mathbf{X}
- Advantages:
 - Minimized variance while maintaining unbiasedness

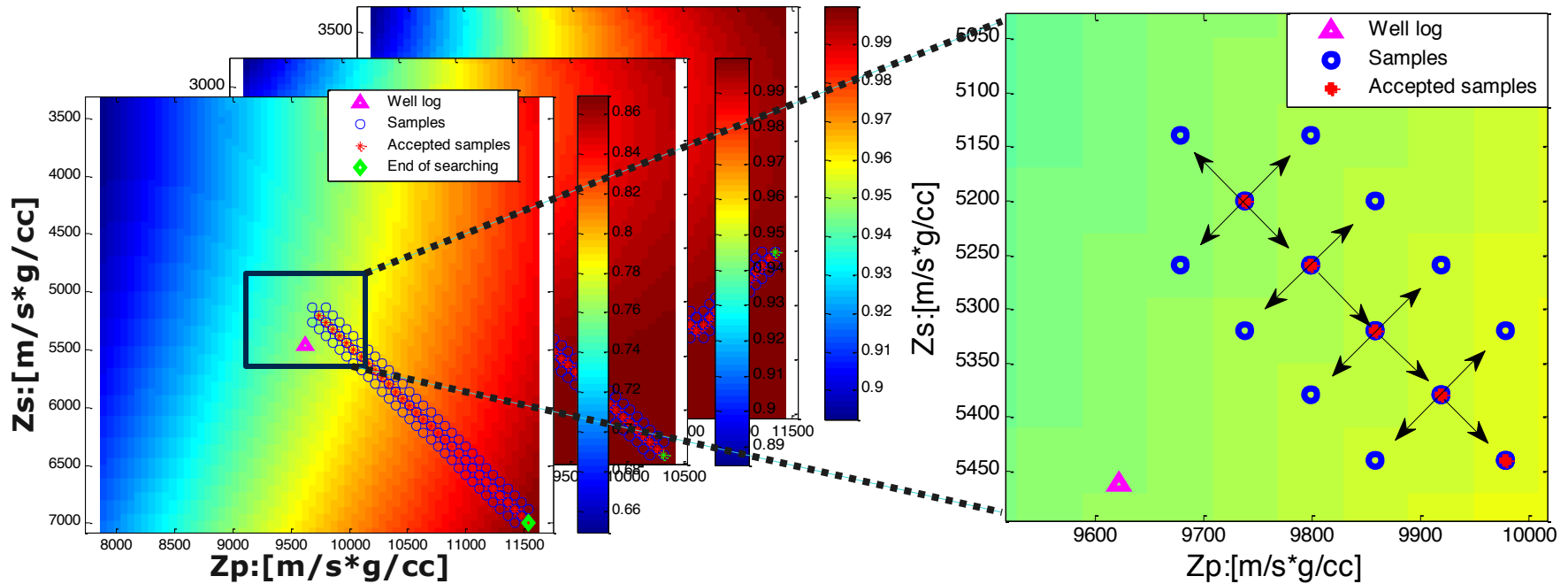
Methodology

Greedy Annealed Importance Sampling - GAIS

- Generate fractal initial model (Srivastava and Sen, 2010)
- Employ multiple VFSA with different starting temperatures and a small number of iterations
- Starting from the best fit model of each VFSA, greedy search important region
 $(\pm\Delta Z_p, \pm\Delta Z_s), (\mp\Delta Z_p, \mp\Delta Z_s)$
- Summation of all weighted samples

Methodology

Visualization of Greedy Search



Marginal probability map of one layer at the well location with multiple runs of VFSA (left box) and zoom in (right). GIS searches within the high probability area step by step. At each step, we compare the importance of the square's ends, whose middle point is our starting point and choose the most important end as a new starting point. Calculation of gradient matrix can also provide the direction of search.

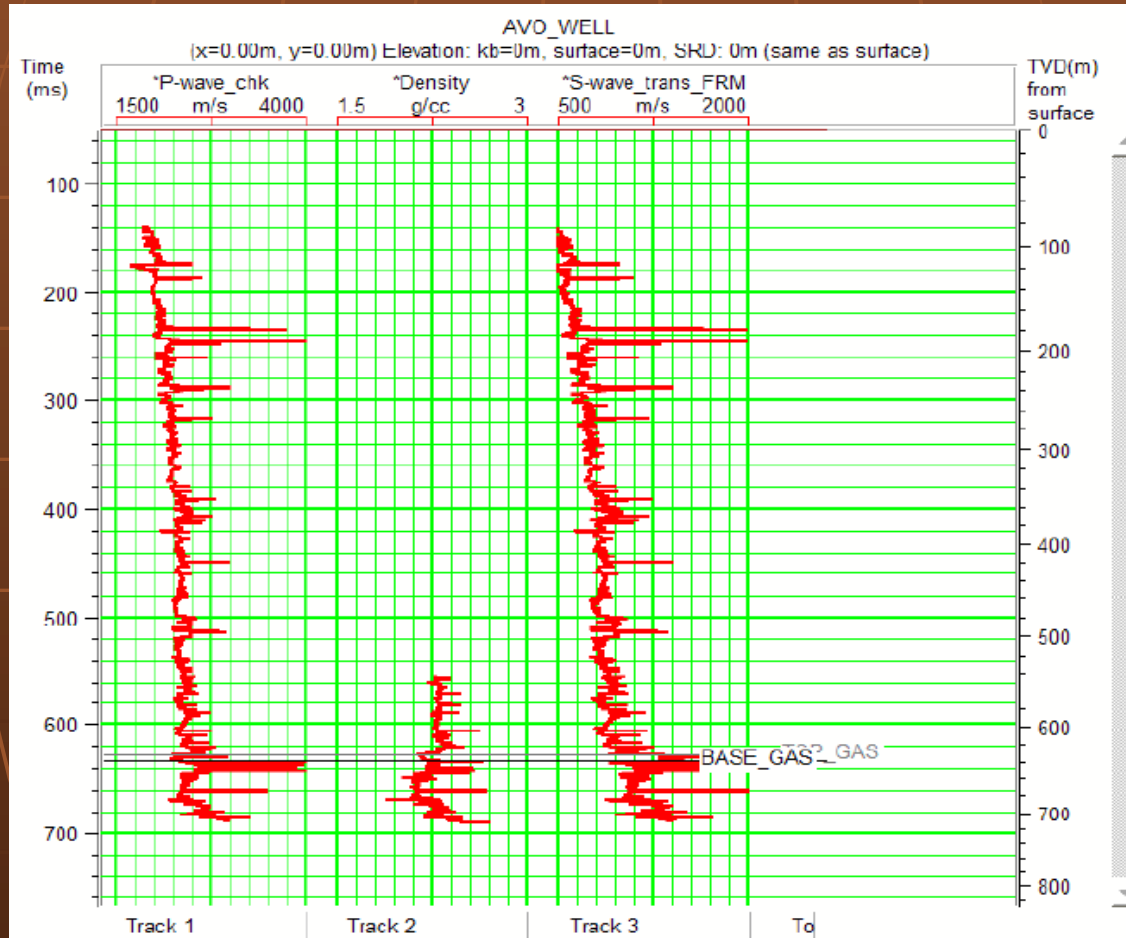
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Application of GAIS

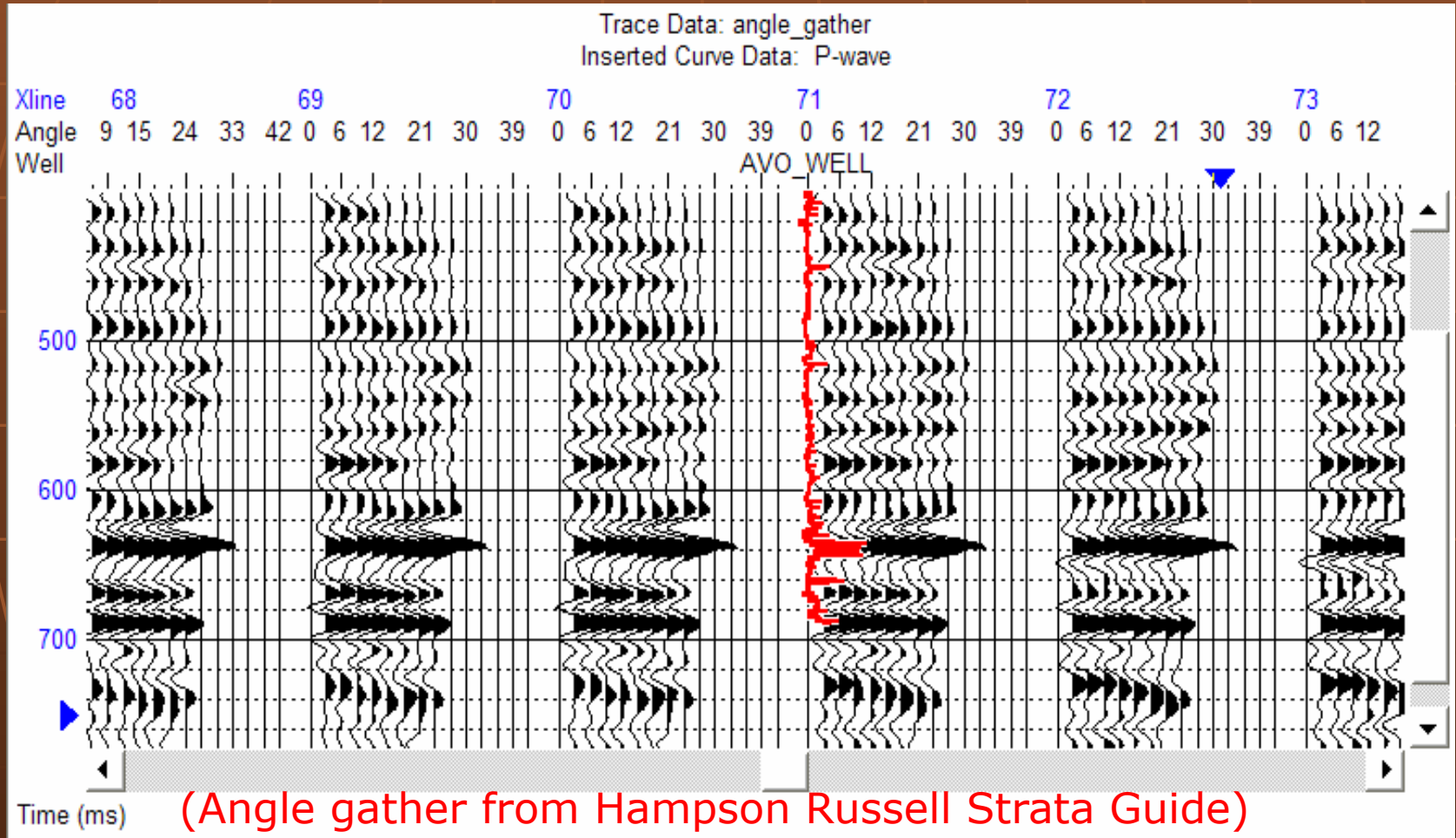
Example 1: HRS demo data (prestack seismic)



Well logs plot
from
Hampson
Russell Strata
Guide

Application of GAIS

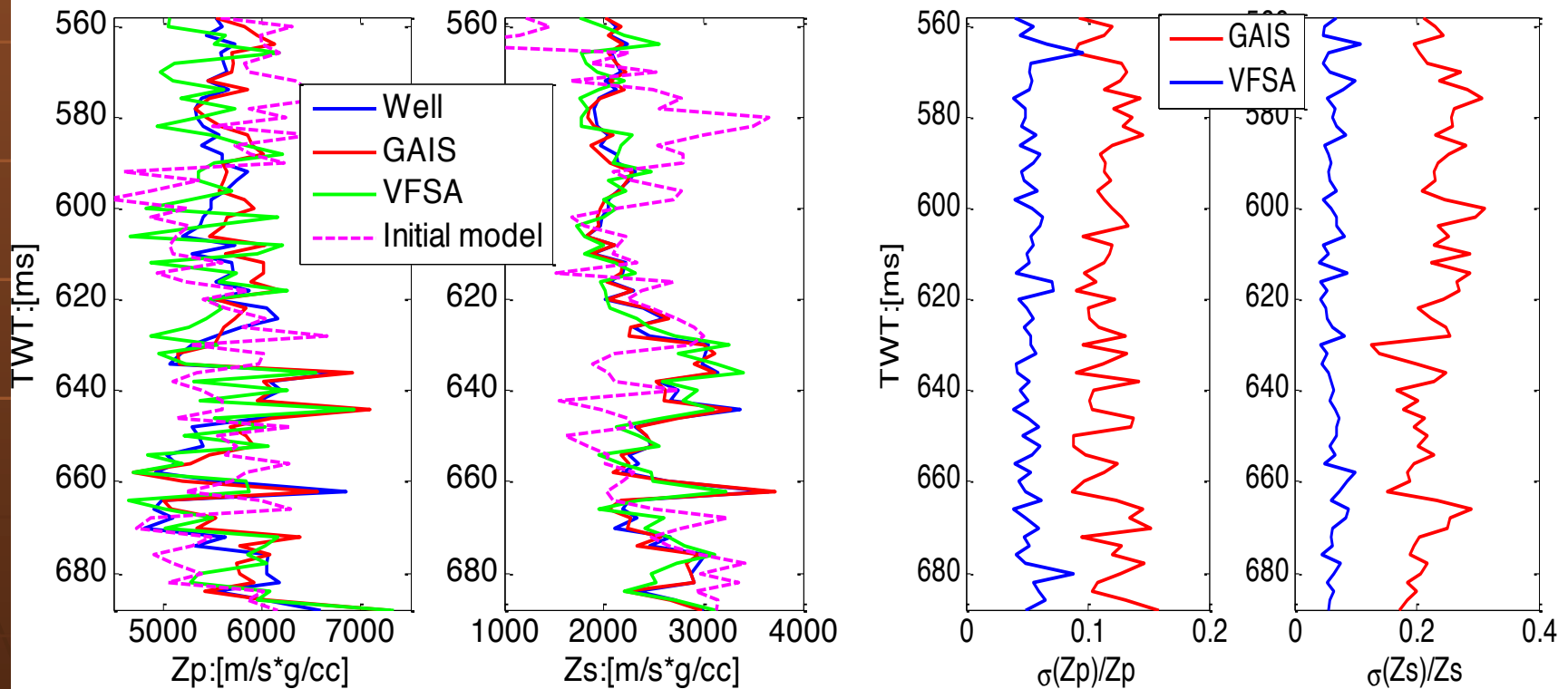
Example 1: HRS demo data (prestack seismic)



Application of GAIS

Example 1: HRS demo data (prestack seismic)

Quality control at the well location



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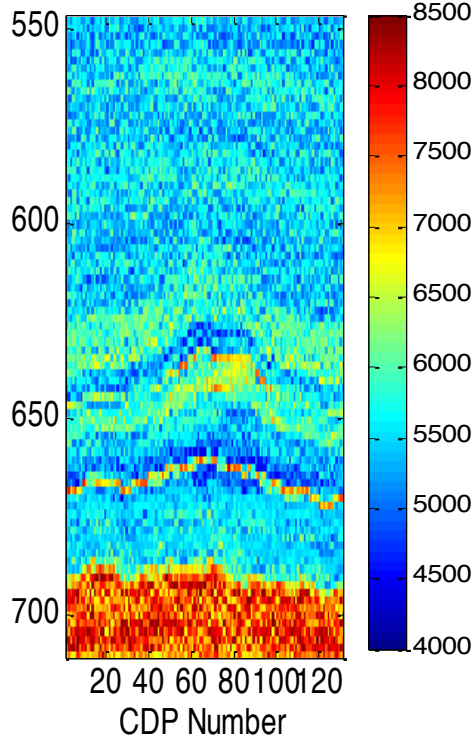
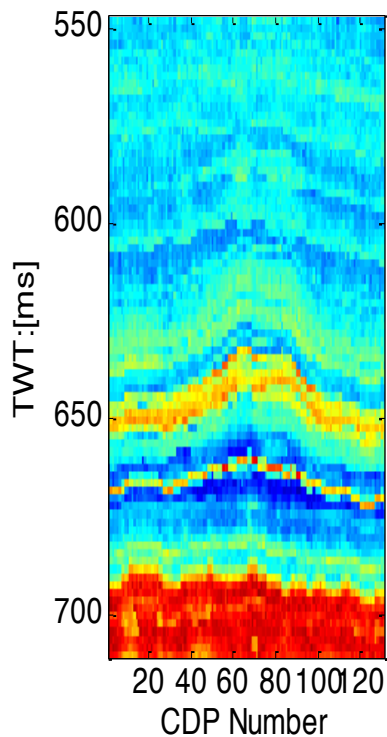
Application of GAIS

Example 1: HRS demo data (prestack seismic)

inverted Z_p

GAIS

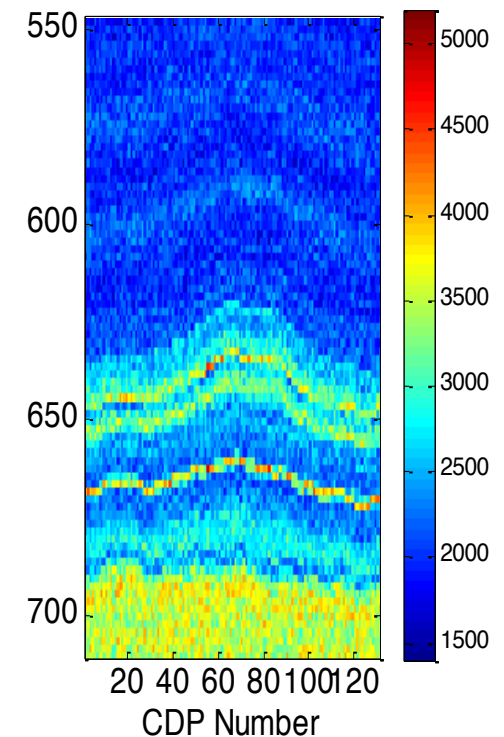
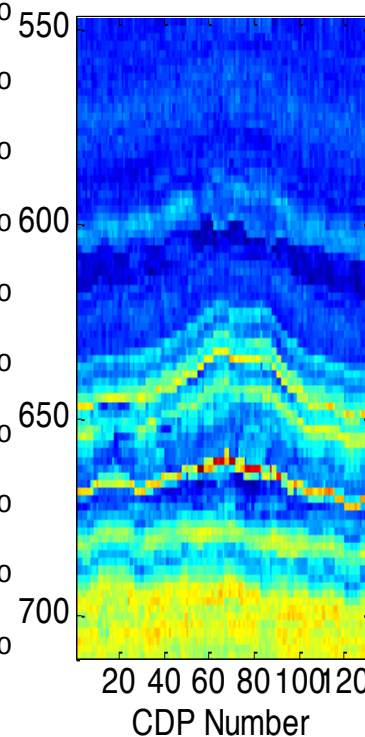
VFSA



inverted Z_s

GAIS

VFSA



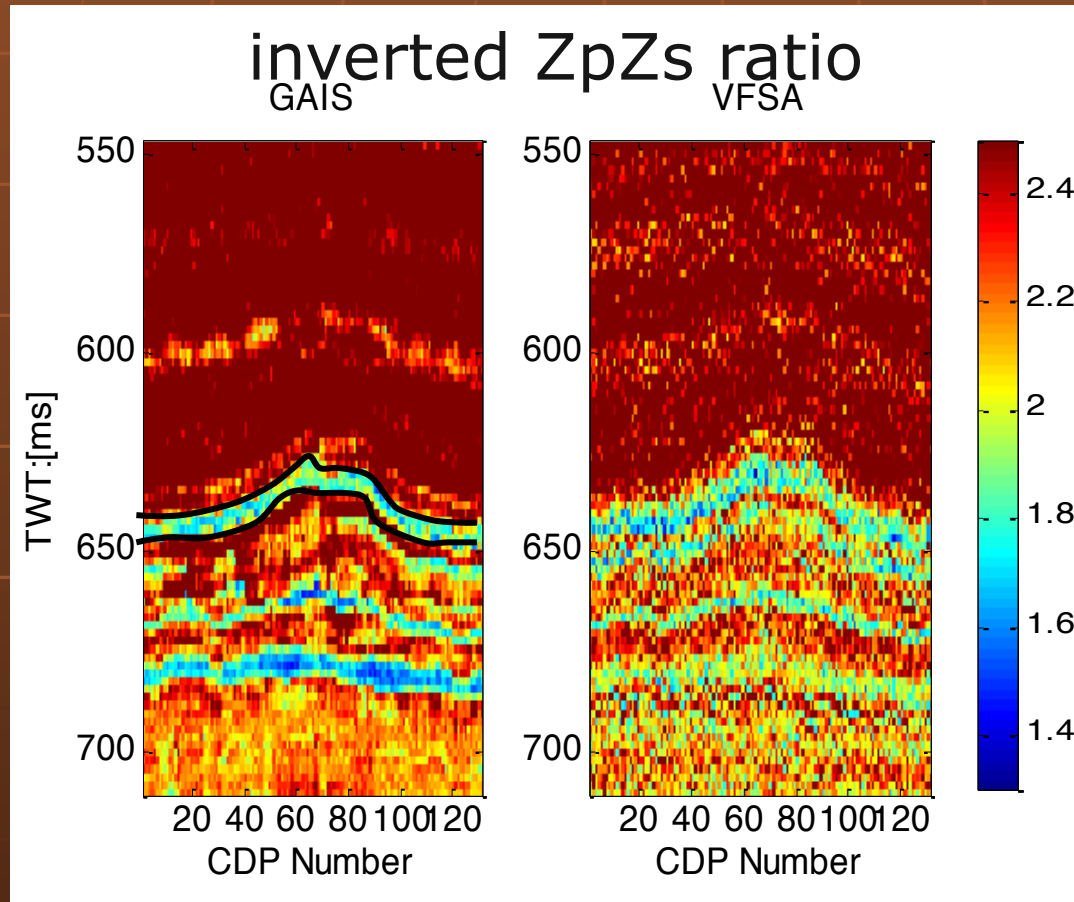
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Application of GAIS

Example 1: HRS demo data (prestack seismic)

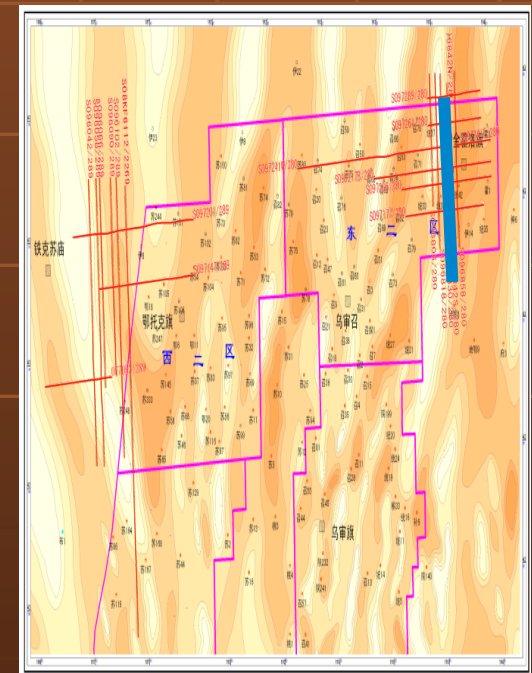
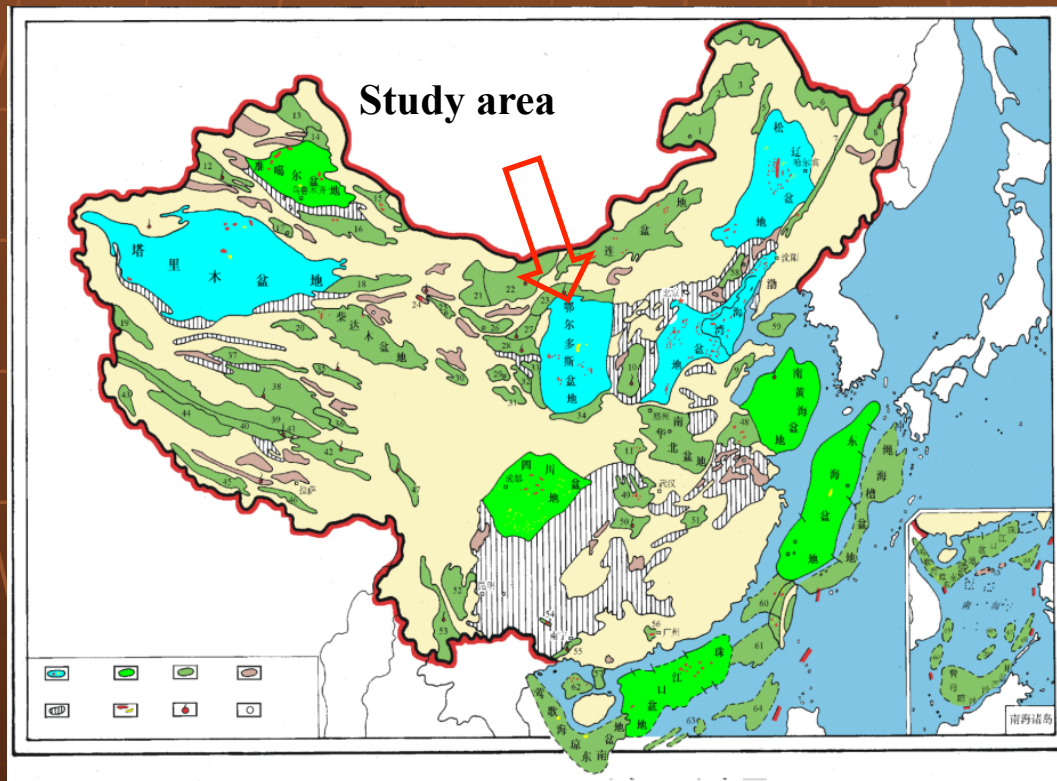


GAIS shows superior Performance than VFSA alone

Application of GAIS

Example 2: Ordos Basin, China (prestack seismic)

Zoomed study area



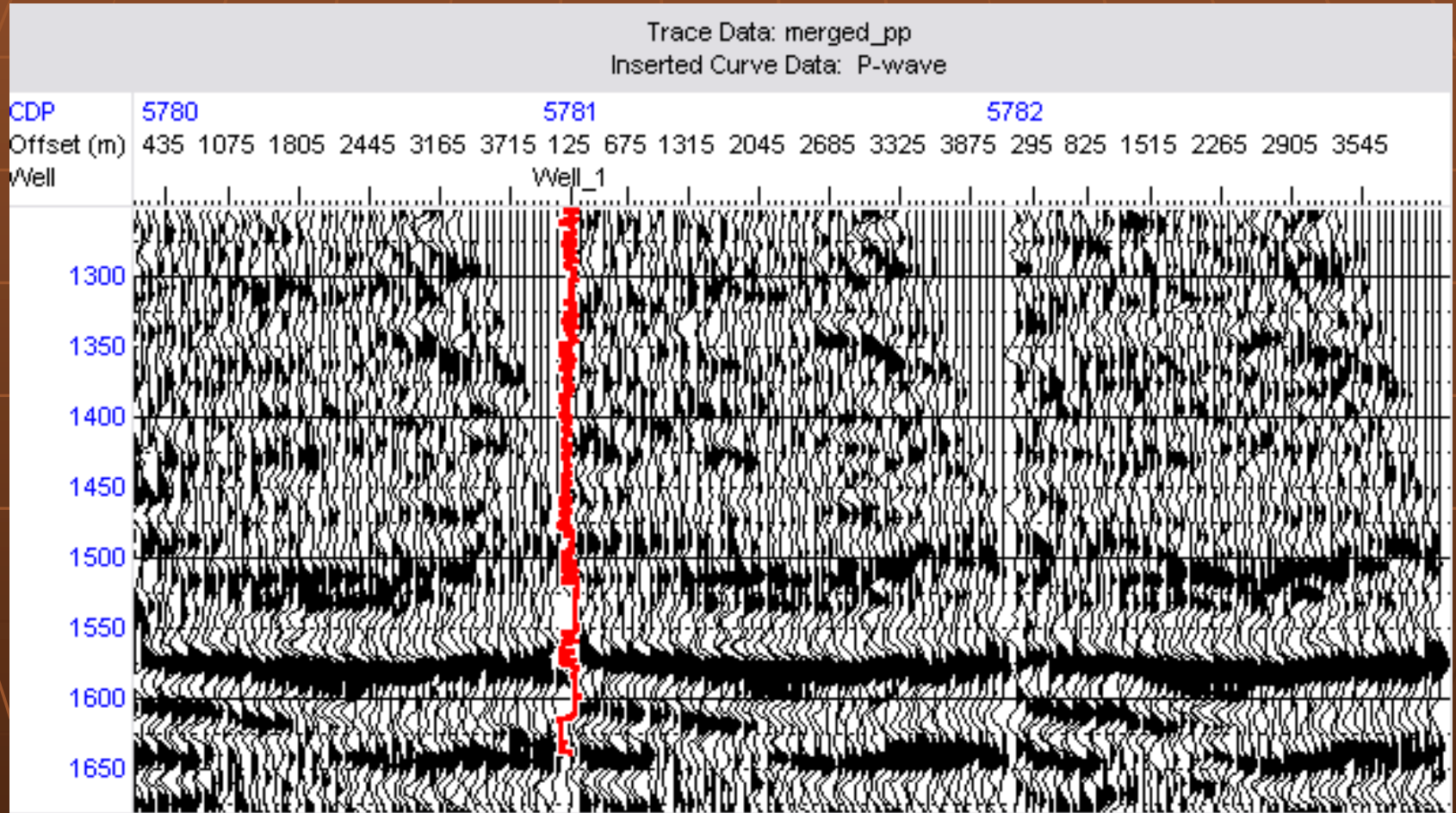
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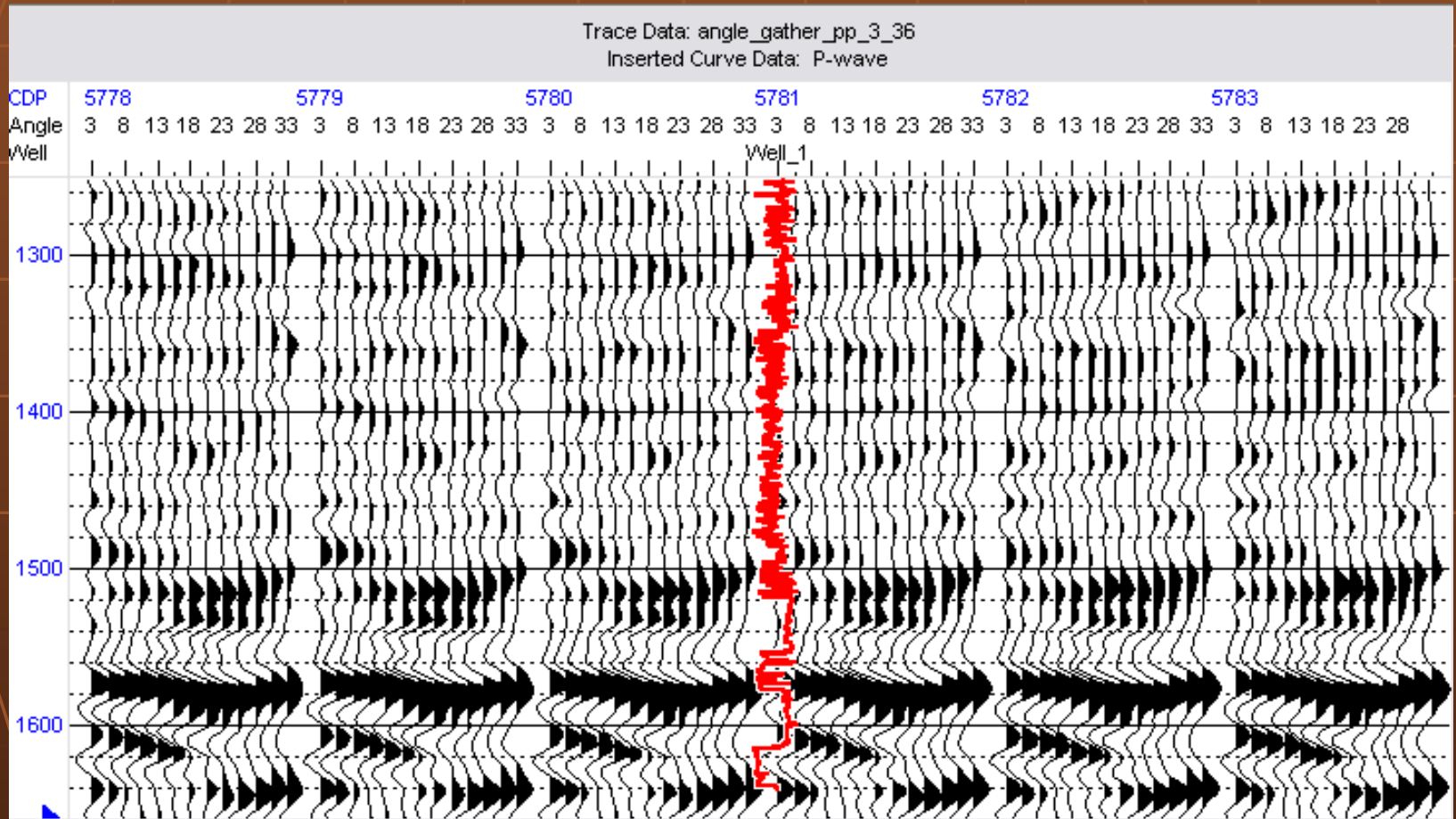
Application of GAIS

Example 2: Ordos Basin, China (prestack seismic)



Application of GAIS

Example 2: Ordos Basin, China (prestack seismic)



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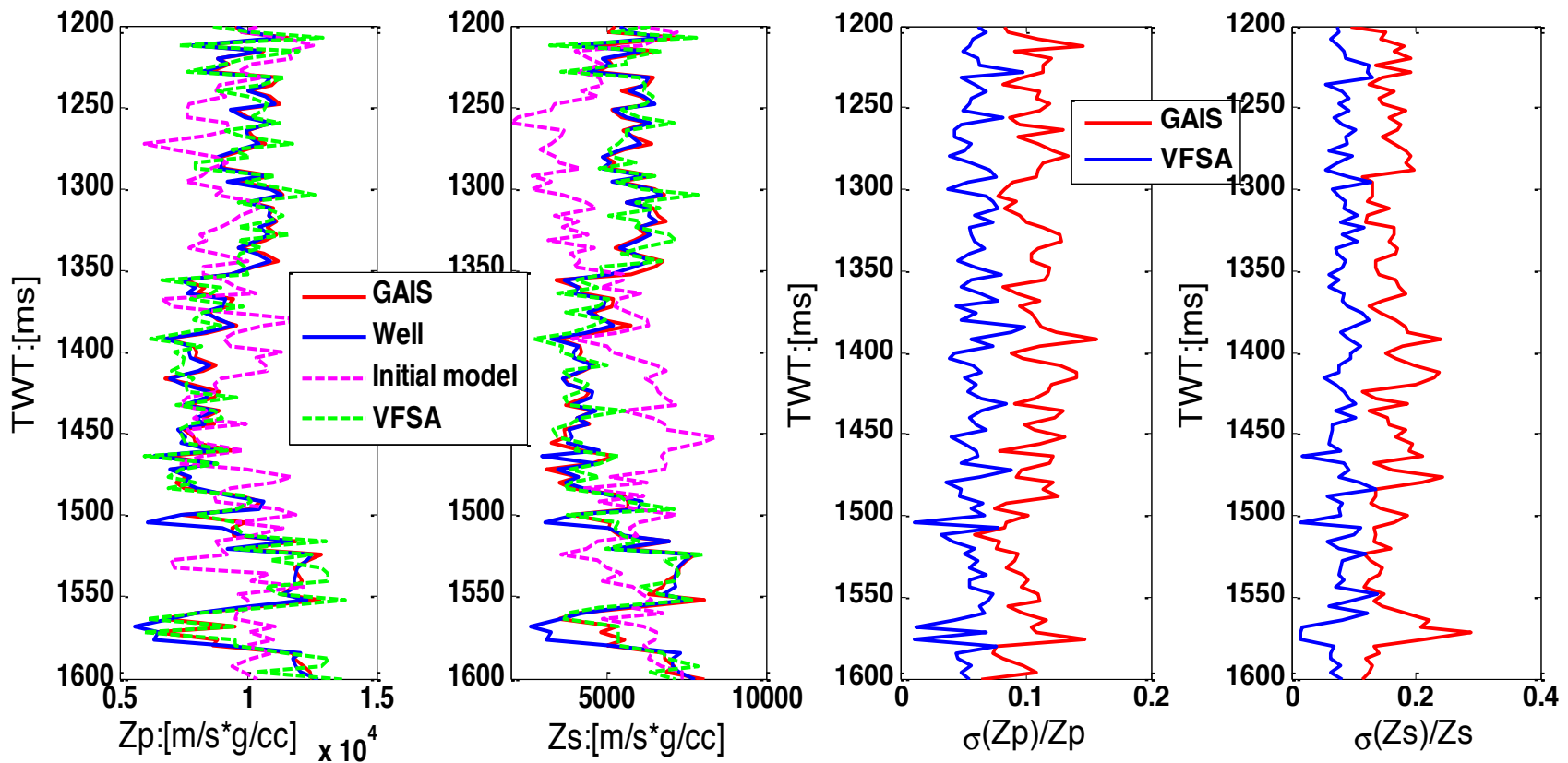
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Application of GAIS

Example 2: Ordos Basin, China (prestack seismic)

Quality control at the well location



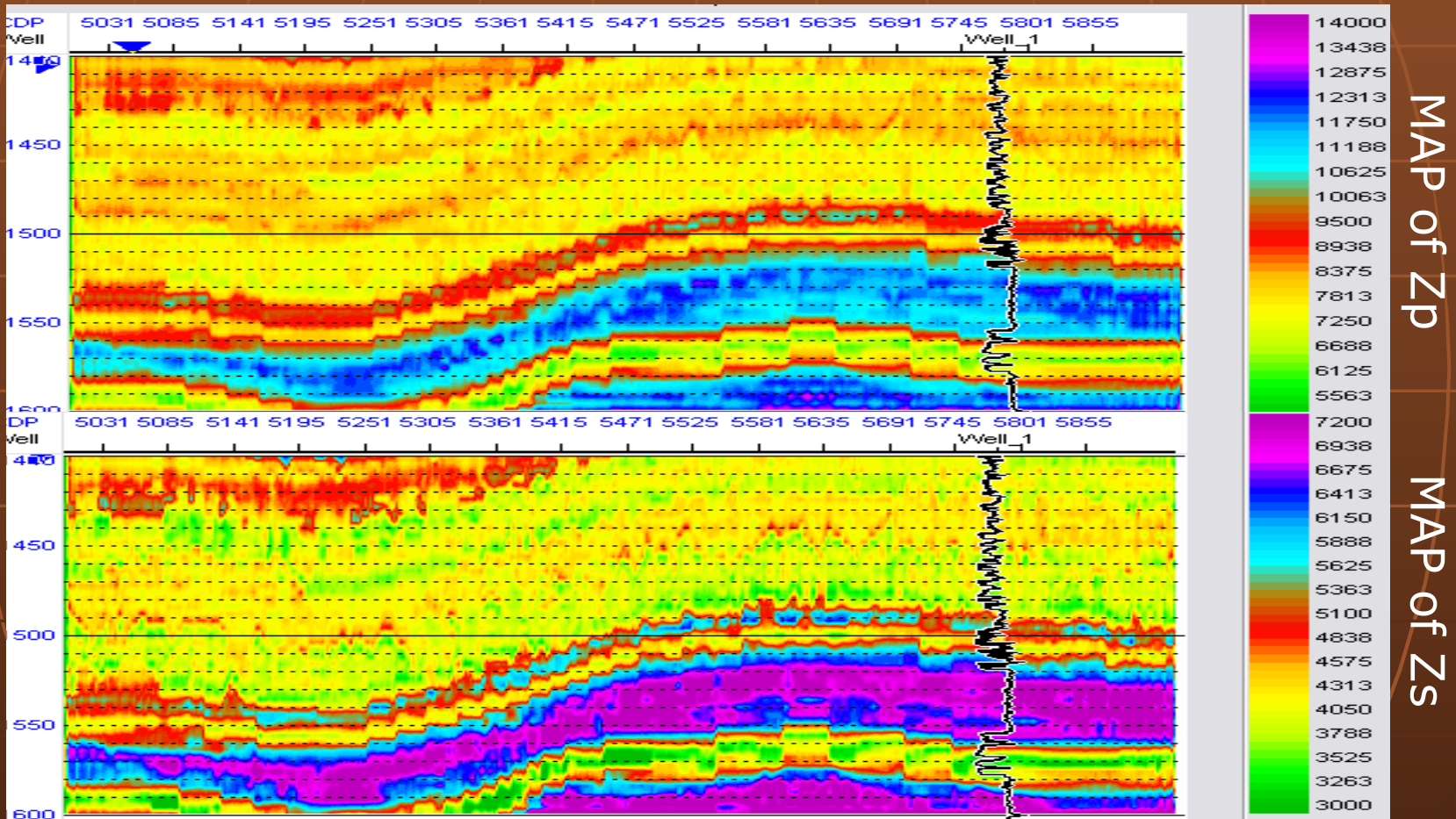
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Application of GAIS

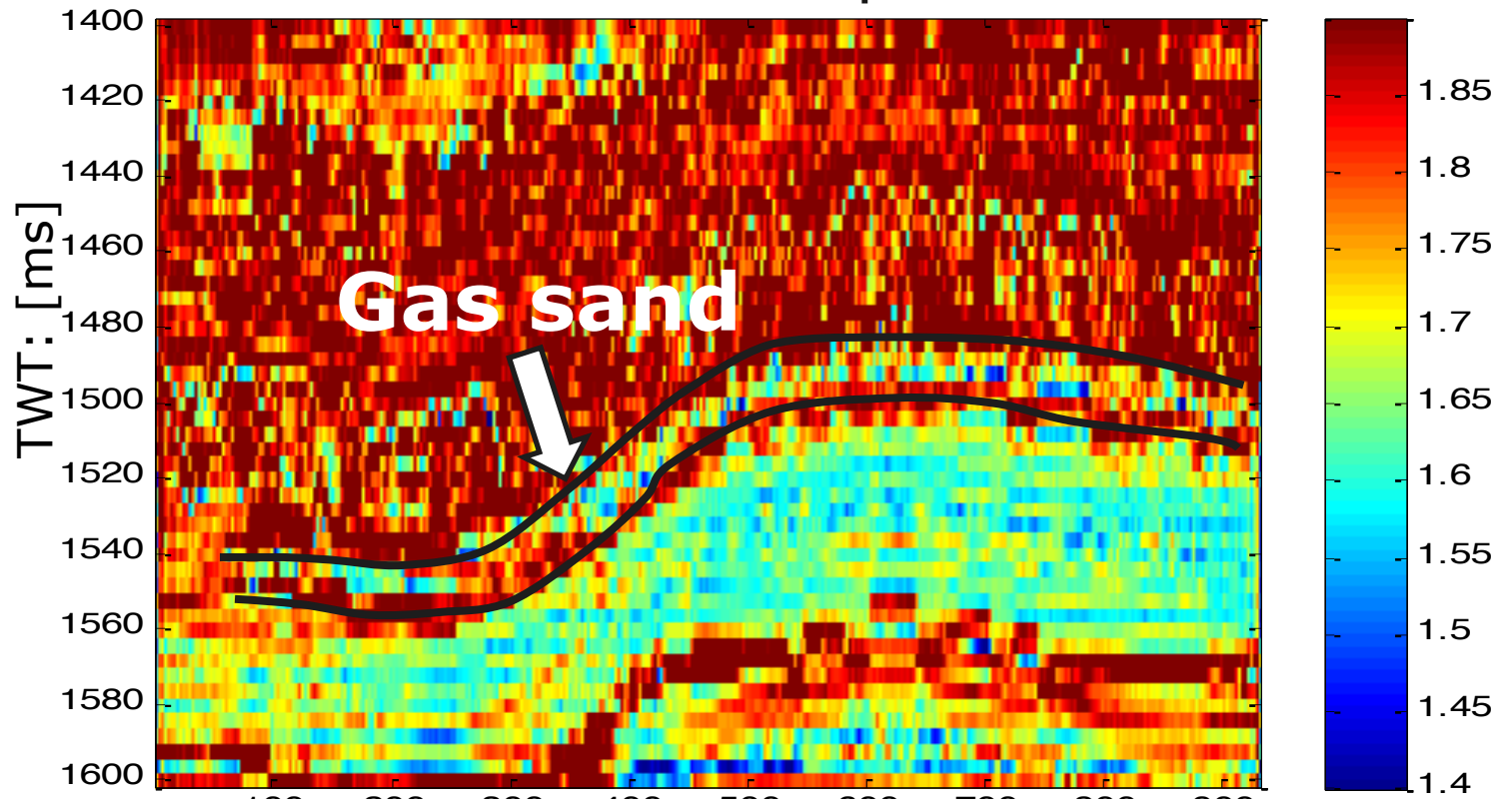
Example 2: Ordos Basin, China (prestack seismic)



Application of GAIS

Example 2: Ordos Basin, China (prestack seismic)

MAP of inverted Z_p/Z_s ratio



Conclusion

- GAIS attempts to explore important regions starting with models that are close to the important regions already located by VFSA and estimates the expectation value very accurately.
- The example of pre-stack inversion demonstrates superior performance of GAIS compared to VFSA alone

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